Math 110 Sect

Midterm 2

Name

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All solutions are to be presented on the exam paper in the space provided. Each question is worth two (2) marks. A disorganized or messy solution will result in a mark of zero for that question. There are nine (9) questions in total on five (5) pages. Time for the exam is 80 minutes.



(1) Compute the following. 1 mark each.

(a) $\tan(\frac{3\pi}{4})$



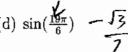
















(2) Find the solution sets for the following. 1 mark each.

(a) $x^2 - 4 > 0$

$$(\chi + 2)(\chi - 2) > 0$$

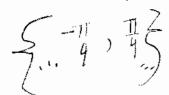
$$\{(-\infty, -2) \cup (2, \infty)\}$$
(b) $\log_2(3-x) = 1$

2 = 3 -X

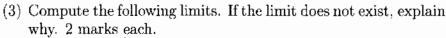
$$-1 = -X$$

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(c) $\sin x = \frac{1}{\sqrt{2}}$ for $x \in [-2\pi, 2\pi]$



(d) $\cos(2x) = 1$ for $x \in [0, 2\pi]$



(a) $\lim_{x\to 1^-} \frac{x^2 + x + 1}{x - 1}$

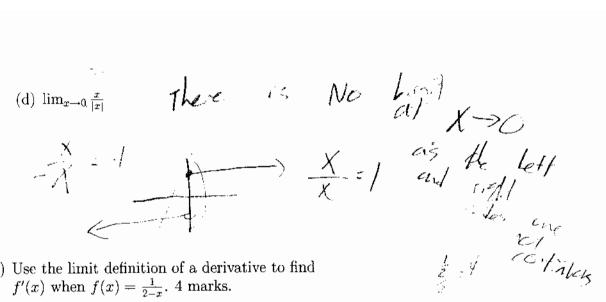


 $= \frac{1}{xT} \qquad As \quad x \to 1^-, \quad f(x) \to \infty$

(b)
$$\lim_{x\to\infty} \frac{\sqrt{x^2+1}}{x+1} \left(\frac{\sqrt{x^2+1}}{1\sqrt{x^2+1}} \right)$$

$$\frac{x^{2}/1}{(x+1)(\sqrt{x})} \to CC$$

(c) $\lim_{x\to 0^-} \log_4(-x)$



(4) Use the limit definition of a derivative to find f'(x) when $f(x) = \frac{1}{2-x}$. 4 marks.

$$\frac{Lm}{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{1}{27(xh)} = \frac{1}{27(xh)}$$

$$= \frac{1}{27(xh)} - \frac{1}{27(xh)}$$

$$= \frac{1}{27(xh)} - \frac{1}{27(xh)}$$

$$= \frac{1}{27(xh)}$$

(5) Compute the derivatives of the following functions. 2 marks cach.

(a)
$$f(x) = 2x^3 - 6x + 1$$

$$= 6x^2 - 6 + 6$$

$$= 6x^2 - 6 = 6 + (x^2 - 1)$$
(b) $f(x) = \frac{x^2 + 1}{2}$

$$\frac{2X(e^{X})-e^{X}(x^{2}H)}{(e^{X})}$$

$$\frac{2X-(X^{2}H)}{e^{X}}$$

(c)
$$f(x) = (x^8 + 4x^2 - 1)(e^x)$$

$$- (8x^2 + 9x)e^x + (x^8 + 9x^2 - 1)(e^x) = e^x (x^8 + 9x^2 + 9x$$

(6) Prove that $\frac{d}{dx}(cx) = c$, c a constant directly from the limit definition of the derivative. 4 marks and a deep sense of satisfaction.

Lim
$$f(x)h - f(x)$$
 $h \to c$
 $f(x)h - f(x)$
 $f(x)h - f(x)$
 $f(x)h + f(x)$

(7) Find the equation of the tangent line to $f(x) = x^2 + 3^x$ at x = 1. 4 marks.

$$f(x) = 2X + (1n3)^{x}$$

$$n = 2 + (n3)$$

$$(2+1n3)(x-1)$$

(8) Let f(1) = 2 and f'(1) = 3 Evaluate the following. 2 marks each.
(a) $\frac{d}{dx} \left(\frac{f(x)}{x} \right) \Big|_{x=1}$.

$$f(x) = \frac{1}{f(x)}$$

$$f(x) = \frac{2-3}{1}$$

(b)
$$\frac{d}{dx}(x^2f(x))|_{x=1}$$

$$2\lambda\left(\frac{1}{x}\right) + \chi^2f(x) = 2 + 3 = 5$$
Where is the following function continuous? Analysis any dis

(9) Where is the following function continuous? Analyze any discontinuities and classify as a removeable, jump, or infinite discontinuity. Sketch the graph of this function. 6 marks.

$$f(x) = \begin{cases} \frac{x^2 - 1}{x - 1} & \text{if } x < 1\\ x^2 & \text{if } x \ge 1 \end{cases}$$

